

Reading: Odomirok - Chapter 22/23
Model: 2016.Fall #18
Problem Type: GAAP goodwill using cost-of-capital approach

(goodwill - practice 01) a-Question

Given

Amounts at time of acquisition at CY	
FV(assets)	690
U.S. GAAP assets	640
FV(liabilities) <i>other than loss & LAE</i>	180
purchase price	108

nominal future cash flows of liabilities	
CY <i>paid during year</i>	230
CY + 1 <i>paid during year</i>	140
CY + 2 <i>paid during year</i>	30
> CY + 2 <i>paid during year</i>	0

some more junk you'll need	
pre-tax cost-of-capital	9%
risk-free rate	3%
illiquidity premium	1%

still more junk you'll need:

loss & LAE payments are made mid-year <== use 0.5, 1.5, 2.5,... to discount
 return on capital is paid to investores at year-end <== use 1, 2, 3,... to discount

required capital @ year-end = **unpaid x** 50%

(stated slightly differently from exam problem - this is done so that my solution fits the risk-adjustment formula from Odomirok)

Find

value of purchaser's GAAP **goodwill** using the cost-of-capital approach

The first section of the solution calculates FV(loss & LAE) according to the 3 components.

(goodwill - practice 01) b-Answer1

Component #1: calculate nominal future cash flows of liabilities

For this problem, we are given the cash flows, otherwise we'd have to calculate them from the LDFs or the payment pattern.

Component #2: discount the nominal cash flows & add a load for illiquidity

$$\begin{aligned} \text{discount rate} &= \text{risk-free rate} + \text{illiquidity premium} \\ &= 3\% + 1\% \\ &= \underline{4\%} \end{aligned}$$

Actually, all we did here was calculate the discount rate, i. The actual discounting is done further down after the risk margin calculation.

Component #3: risk margin calculation

First, we need the cumulative unpaid values at the start of each year. See table at right =>

CY	400
CY + 1	170
CY + 2	30
> CY + 2	0

Then the capital required to support these liabilities = 50% x unpaid:

$$\begin{aligned} C_0 &= 50\% \times 400 = 200 \\ C_1 &= 50\% \times 170 = 85 \\ C_2 &= 50\% \times 30 = 15 \\ C_3 &= 50\% \times 0 = 0 \end{aligned}$$

Now we can apply the **risk adjustment** formula using the discount rate from above:

Note that we use integer exponents because investors are paid at year-end.

$$\begin{aligned} \text{avg}(C_0, C_1) &/ (1.04)^1 = 137.0 \\ \text{avg}(C_1, C_2) &/ (1.04)^2 = 46.2 \\ \text{avg}(C_2, C_3) &/ (1.04)^3 = 6.7 \\ \text{avg}(C_3, C_4) &/ (1.04)^4 = 0.0 \\ &\underline{189.9} \\ &\times 5\% = (R - i) \\ &\text{risk margin component of FV(liabilities)} \Rightarrow \underline{9.5} \end{aligned}$$

solution continued on next page...

Now we have to calculate the discounted **unpaid values** using the same discount rate
 Use the given **incremental** unpaid values.

(goodwill - practice 01) b-Answer2

Note that we use fractional exponents 0.5, 1.5, 2.5,... because payments are made mid-year.

230	/	(1.04) ^ 0.5	=	225.5
140	/	(1.04) ^ 1.5	=	132.0
30	/	(1.04) ^ 2.5	=	27.2
				384.7

Now we have all the pieces of FV(liabilities)

risk margin	9.5	
unpaid loss & LAE:	384.7	
other than loss & LAE:	180.0	<i><== given in the statement of the problem</i>
FV(liabilities) =	574.2	

We also know: **FV(assets) = 690.0** *<== given in the statement of the problem*
P = 108.0 *<== given in the statement of the problem*

Then: *(purchase price)*

goodwill	=	P	-	[FV(assets)	-	FV(liabs)]
	=	108.0	-	[690.0	-	574.2]
	=	-7.8						<i><== final answer</i>

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(goodwill - practice 02) a-Question

Given

Amounts at time of acquisition at CY	
FV(assets)	500
U.S. GAAP assets	520
FV(liabilities) <i>other than loss & LAE</i>	130
purchase price	70

nominal future cash flows of liabilities	
CY <i>paid during year</i>	180
CY + 1 <i>paid during year</i>	100
CY + 2 <i>paid during year</i>	30
> CY + 2 <i>paid during year</i>	0

some more junk you'll need	
pre-tax cost-of-capital	8%
risk-free rate	2%
illiquidity premium	1%

still more junk you'll need:

loss & LAE payments are made mid-year
 return on capital is paid to investores at year-end

<== use 0.5, 1.5, 2.5,... to discount

<== use 1, 2, 3,... to discount

required capital @ year-end = **unpaid x** 50%

(stated slightly differently from exam problem - this is done so that my solution fits the risk-adjustment formula from Odomirok)

Find

value of purchaser's GAAP **goodwill** using the cost-of-capital approach

The first section of the solution calculates FV(loss & LAE) according to the 3 components.

(goodwill - practice 02) b-Answer1

Component #1: calculate nominal future cash flows of liabilities

For this problem, we are given the cash flows, otherwise we'd have to calculate them from the LDFs or the payment pattern.

Component #2: discount the nominal cash flows & add a load for illiquidity

$$\begin{aligned} \text{discount rate} &= \text{risk-free rate} + \text{illiquidity premium} \\ &= 2\% + 1\% \\ &= \underline{3\%} \end{aligned}$$

Actually, all we did here was calculate the discount rate, i. The actual discounting is done further down after the risk margin calculation.

Component #3: risk margin calculation

First, we need the cumulative unpaid values at the start of each year. See table at right =>

CY	310
CY + 1	130
CY + 2	30
> CY + 2	0

Then the capital required to support these liabilities = 50% x unpaid:

$$\begin{aligned} C_0 &= 50\% \times 310 = 155 \\ C_1 &= 50\% \times 130 = 65 \\ C_2 &= 50\% \times 30 = 15 \\ C_3 &= 50\% \times 0 = 0 \end{aligned}$$

Now we can apply the **risk adjustment** formula using the discount rate from above:

Note that we use integer exponents because investors are paid at year-end.

$$\begin{aligned} \text{avg}(C_0, C_1) &/ (1.03)^1 = 106.8 \\ \text{avg}(C_1, C_2) &/ (1.03)^2 = 37.7 \\ \text{avg}(C_2, C_3) &/ (1.03)^3 = 6.9 \\ \text{avg}(C_3, C_4) &/ (1.03)^4 = 0.0 \\ &\quad \quad \quad 151.4 \\ &\quad \quad \quad \times 5\% = (R - i) \\ &\quad \quad \quad \text{risk margin component of FV(liabilities)} \Rightarrow \underline{7.6} \end{aligned}$$

solution continued on next page...

Now we have to calculate the discounted **unpaid values** using the same discount rate
 Use the given **incremental** unpaid values.

(goodwill - practice 02) b-Answer2

Note that we use fractional exponents 0.5, 1.5, 2.5,... because payments are made mid-year.

180	/	(1.03) ^ 0.5	=	177.4
100	/	(1.03) ^ 1.5	=	95.7
30	/	(1.03) ^ 2.5	=	27.9
				300.9

Now we have all the pieces of FV(liabilities)

risk margin	7.6	
unpaid loss & LAE:	300.9	
other than loss & LAE:	130.0	<i><== given in the statement of the problem</i>
FV(liabilities) =	438.5	

We also know: **FV(assets) = 500.0** *<== given in the statement of the problem*
P = 70.0 *<== given in the statement of the problem*

Then: *(purchase price)*

goodwill	=	P	-	[FV(assets)	-	FV(liabs)]
	=	70.0	-	[500.0	-	438.5]
	=	8.5						<i><== final answer</i>