

Reading: Klann.ReinsComm (Reinsurance (Model - 2017.Fall Q27b)) 01a-Question
Model: 2017.Fall #27b
Problem Type: restate triangles after commutation

Given

Primary Insurer

Ceded Paid Losses without Commutation			
policy year	12	24	36
PY-2	1,200	1,550	1,710
PY-1	1,000	1,320	
PY	800		

In the exam problem, PY = 2016

Primary Insurer

Net Reserves without Commutation			
policy year	12	24	36
PY-2	900	660	460
PY-1	600	480	
PY	700		

quota-share %	60%
commutation price:	600

Problem

The insurer has decided to commute this contract for PY-2 within the latest calendar year.

- i Restate the primary insurer's **net paid** loss triangle after commutation.
- ii Restate the primary insurer's **net ultimate** loss triangle after commutation.

Hint 1:

State the desired triangles **without** commutation, then make the appropriate adjustments.

Hint 2:

Identify that cells in the triangle that are impacted by the commutation:
 ==> the only cell that is impacted is PY-2 & 36 months

Note: $\frac{\text{gross pd}}{\text{net pd}} = \frac{\text{ceded pd}}{\text{gross pd} \times (1 - \text{qs\%})}$

$\Rightarrow \text{net pd} = \frac{\text{ceded pd} \times (1 - \text{qs\%})}{\text{qs\%}}$

Primary Insurer

Net Paid Losses <i>without</i> Commutation			
policy year	12	24	36
PY-2	800	1,033	1,140
PY-1	667	880	
PY	533		

Step 1:

- use the above formula to create the net paid triangle without commutation (*on left*)

Step 2:

- adjust the appropriate entry from Step 1 (*see below*)

Primary Insurer (this is the answer to part i)

Net Paid Losses <i>with</i> Commutation			
policy year	12	24	36
PY-2	800	1,033	540
PY-1	667	880	
PY	533		

$$= 1,140 - \frac{\text{commutation price}}{600}$$

For part ii, proceed as follows:

Primary Insurer

Net Ultimate Losses <i>without</i> Commutation			
policy year	12	24	36
PY-2	1,700	1,693	1,600
PY-1	1,267	1,360	
PY	1,233		

Step 1:

- compute net **ultimate** loss triangle without commutation by summing net paid loss & net reserve (*on left*)

Step 2:

- adjust the appropriate entry from Step 1 (*see below*)

Primary Insurer

Net Ultimate Losses <i>with</i> Commutation			
policy year	12	24	36
PY-2	1,700	1,693	1,690
PY-1	1,267	1,360	
PY	1,233		

$$= \frac{\text{paid loss with commutation}}{540} + \frac{\text{net resv without commutation}}{460} + \frac{\text{ceded resv without commutation}}{690}$$

Note: $\frac{\text{gross resv}}{\text{ceded resv}} = \frac{\text{net resv}}{\text{gross resv} \times (1 - \text{qs\%})}$

$\Rightarrow \text{ceded resv} = \frac{\text{net resv} \times \text{qs\%}}{(1 - \text{qs\%})}$