

Reading: Klann.ReinsComm (Reinsurance (Model - 2017.Fall Q27b)) 01a-Question
Model: 2017.Fall #27b
Problem Type: restate triangles after commutation

Given

Primary Insurer

Ceded Paid Losses without Commutation			
policy year	12	24	36
PY-2	900	990	1,080
PY-1	900	990	
PY	900		

In the exam problem, PY = 2016

Primary Insurer

Net Reserves without Commutation			
policy year	12	24	36
PY-2	1,200	800	400
PY-1	1,200	800	
PY	1,200		

quota-share %	90%
commutation price:	100

Problem

The insurer has decided to commute this contract for PY-2 within the latest calendar year.

- i Restate the primary insurer's **net paid** loss triangle after commutation.
- ii Restate the primary insurer's **net ultimate** loss triangle after commutation.

Hint 1:

State the desired triangles **without** commutation, then make the appropriate adjustments.

Hint 2:

Identify that cells in the triangle that are impacted by the commutation:
 ==> the only cell that is impacted is PY-2 & 36 months

Note: $\text{gross pd} = \text{ceded pd} / \text{qs\%}$
 $\text{net pd} = \text{gross pd} \times (1 - \text{qs\%})$

$\Rightarrow \text{net pd} = \text{ceded pd} \times (1 - \text{qs\%}) / \text{qs\%}$

Primary Insurer

Net Paid Losses <i>without</i> Commutation			
policy year	12	24	36
PY-2	100	110	120
PY-1	100	110	
PY	100		

Step 1:

- use the above formula to create the net paid triangle without commutation (*on left*)

Step 2:

- adjust the appropriate entry from Step 1 (*see below*)

Primary Insurer (this is the answer to part i)

Net Paid Losses <i>with</i> Commutation			
policy year	12	24	36
PY-2	100	110	20
PY-1	100	110	
PY	100		

$$= 120 - \frac{\text{commutation price}}{100}$$

For part ii, proceed as follows:

Primary Insurer

Net Ultimate Losses <i>without</i> Commutation			
policy year	12	24	36
PY-2	1,300	910	520
PY-1	1,300	910	
PY	1,300		

Step 1:

- compute net **ultimate** loss triangle without commutation by summing net paid loss & net reserve (*on left*)

Step 2:

- adjust the appropriate entry from Step 1 (*see below*)

Primary Insurer

Net Ultimate Losses <i>with</i> Commutation			
policy year	12	24	36
PY-2	1,300	910	4,020
PY-1	1,300	910	
PY	1,300		

$$= \begin{array}{c} \text{paid loss} \\ \text{with} \\ \text{commutation} \end{array} 20 + \begin{array}{c} \text{net resv} \\ \text{without} \\ \text{commutation} \end{array} 400 + \begin{array}{c} \text{ceded resv} \\ \text{without} \\ \text{commutation} \end{array} 3600$$

Note: $\text{gross resv} = \text{net resv} / (1 - \text{qs\%})$
 $\text{ceded resv} = \text{gross resv} \times \text{qs\%}$

$\Rightarrow \text{ceded resv} = \text{net resv} \times \text{qs\%} / (1 - \text{qs\%})$