

Reading: Klann.ReinsComm (Reinsurance (Model - 2017.Fall Q27b)) 01a-Question
Model: 2017.Fall #27b
Problem Type: restate triangles after commutation

Given

Primary Insurer

Ceded Paid Losses without Commutation			
policy year	12	24	36
PY-2	250	350	450
PY-1	250	350	
PY	250		

In the exam problem, PY = 2016

Primary Insurer

Net Reserves without Commutation			
policy year	12	24	36
PY-2	1,500	1,200	900
PY-1	1,500	1,200	
PY	1,500		

quota-share %	25%
commutation price:	250

Problem

The insurer has decided to commute this contract for PY-2 within the latest calendar year.

- i Restate the primary insurer's **net paid** loss triangle after commutation.
- ii Restate the primary insurer's **net ultimate** loss triangle after commutation.

Hint 1:

State the desired triangles **without** commutation, then make the appropriate adjustments.

Hint 2:

Identify that cells in the triangle that are impacted by the commutation:
 ==> the only cell that is impacted is PY-2 & 36 months

Note: $\text{gross pd} = \text{ceded pd} / \text{qs\%}$
 $\text{net pd} = \text{gross pd} \times (1 - \text{qs\%})$

$\Rightarrow \text{net pd} = \text{ceded pd} \times (1 - \text{qs\%}) / \text{qs\%}$

Primary Insurer

Net Paid Losses <i>without</i> Commutation				
policy year	12	24	36	
PY-2	750	1,050	1,350	
PY-1	750	1,050		
PY	750			

Step 1:

- use the above formula to create the net paid triangle without commutation (*on left*)

Step 2:

- adjust the appropriate entry from Step 1 (*see below*)

Primary Insurer (this is the answer to part i)

Net Paid Losses <i>with</i> Commutation				
policy year	12	24	36	
PY-2	750	1,050	1,100	
PY-1	750	1,050		
PY	750			

$$= 1,350 - \frac{\text{commutation price}}{250}$$

For part ii, proceed as follows:

Primary Insurer

Net Ultimate Losses <i>without</i> Commutation				
policy year	12	24	36	
PY-2	2,250	2,250	2,250	
PY-1	2,250	2,250		
PY	2,250			

Step 1:

- compute net **ultimate** loss triangle without commutation by summing net paid loss & net reserve (*on left*)

Step 2:

- adjust the appropriate entry from Step 1 (*see below*)

Primary Insurer

Net Ultimate Losses <i>with</i> Commutation				
policy year	12	24	36	
PY-2	2,250	2,250	2,300	
PY-1	2,250	2,250		
PY	2,250			

$$= \frac{\text{paid loss with commutation}}{1,100} + \frac{\text{net resv without commutation}}{900} + \frac{\text{ceded resv without commutation}}{300}$$

Note: $\text{gross resv} = \text{net resv} / (1 - \text{qs\%})$
 $\text{ceded resv} = \text{gross resv} \times \text{qs\%}$

$\Rightarrow \text{ceded resv} = \text{net resv} \times \text{qs\%} / (1 - \text{qs\%})$