

Reading: Klann.ReinsComm
Model: 2017.Spring #26b
Problem Type: change in taxable income

(tax effect HARD - Ex 1) x-Question

Given The following pertains to a reinsurance contract that was commuted:

quota-share percentage	70%		
primary insurer RESERVE direct(net)	1,100,000	=	${}_p\bar{R}_{gross}$
primary insurer ULTIMATE direct(net)	1,900,000	=	${}_p\bar{U}_{gross}$
discount factor for primary insurer	0.820		
discount factor for reinsurer	0.880		

REINSURER'S carried loss reserves (prior to commutation)
 are higher than the INSURED'S carried reserves by: -6%

REINSURER'S ultimate loss reserves, as a result of
 commutation, increased by: -5%

Find change in taxable income for both insurer and reinsurer

Notation
 P = commutation price
 ${}_p\bar{R}_{ceded}$ = CEDED carried reserve for primary insurer
 ${}_{re}\bar{R}_{gross}$ = GROSS carried reserve for reinsurer
 d_1 = discount factor for primary insurer
 d_2 = discount factor for reinsurer

Formulas
 change in taxable income for primary insurer = price - $({}_p\bar{R}_{ceded}) \times d_1$
 change in taxable income for reinsurer = $({}_{re}\bar{R}_{gross}) \times d_2$ - price

insurer	=	28,210	(increase)
reinsurer	=	-22,666	(decrease)

(tax effect HARD - Ex 1) y-Answer

70% quota-share reinsurance means that 70% is CEDED to reinsurer:

pR_{ceded}^-	=	pR_{gross}^-	x	qs%	=	
	=	1,100,000	x	70%	=	770,000
reR_{gross}^-	=	pR_{ceded}^-	x	0.94	=	
	=	770,000	x	0.94	=	723,800

The hard part of this problem is calculating the commutation price P:

pP_{gross}^-	=	primary insurer PAID LOSS direct	=	pU_{gross}^-	-	pR_{gross}^-
	=		=	1,900,000	-	1,100,000
	=		=	800,000		
pP_{ceded}^-	=	primary insurer PAID LOSS ceded	=	pP_{gross}^-	x	qs%
(also equals reP_{gross}^-)			=	800,000	x	70%
	=		=	560,000		
	=		=	reP_{gross}^-	(reinsurer PAID LOSS gross)	
reU_{gross}^-	=	reinsurer ULTIMATE LOSS gross	=	reP_{gross}^-	+	reR_{gross}^-
	=		=	560,000	+	723,800
	=		=	1,283,800		

But this is the GROSS ultimate loss PRIOR to commutation. **AFTER** commutation, we have:

reU_{gross}^+	=	reinsurer ULTIMATE LOSS gross	=	reU_{gross}^-	x	95%
	=		=	1,283,800	x	95%
	=		=	1,219,610		

now, reinsurer's reserve goes to 0, and the "extra" money in the ultimate must be the commutation price:

price	=	1,219,610	-	560,000
	=	659,610		

We now have what we need to substitute into the **given formulas** for change in taxable income:

change in taxable income for primary insurer	=	28,210	(increase)
change in taxable income for reinsurer	=	-22,666	(decrease)

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(tax effect HARD - Ex 2) x-Question

Given The following pertains to a reinsurance contract that was commuted:

quota-share percentage	30%		
primary insurer RESERVE direct(net)	1,200,000	=	${}_p\bar{R}_{gross}$
primary insurer ULTIMATE direct(net)	1,840,000	=	${}_p\bar{U}_{gross}$
discount factor for primary insurer	0.860		
discount factor for reinsurer	0.910		

REINSURER'S carried loss reserves (prior to commutation)
 are higher than the INSURED'S carried reserves by: 2%

REINSURER'S ultimate loss reserves, as a result of
 commutation, increased by: 4%

Find change in taxable income for both insurer and reinsurer

Notation
 P = commutation price
 ${}_p\bar{R}_{ceded}$ = CEDED carried reserve for primary insurer
 ${}_{re}\bar{R}_{gross}$ = GROSS carried reserve for reinsurer
 d_1 = discount factor for primary insurer
 d_2 = discount factor for reinsurer

Formulas
 change in taxable income for primary insurer = price - $({}_p\bar{R}_{ceded}) \times d_1$
 change in taxable income for reinsurer = $({}_{re}\bar{R}_{gross}) \times d_2$ - price

$$\begin{aligned} \text{insurer} &= 79,968 \text{ (increase)} \\ \text{reinsurer} &= -55,416 \text{ (decrease)} \end{aligned}$$

(tax effect HARD - Ex 2) y-Answer

30% quota-share reinsurance means that 30% is CEDED to reinsurer:

$$\begin{aligned} pR_{ceded}^- &= pR_{gross}^- \times qs\% \\ &= 1,200,000 \times 30\% = 360,000 \\ reR_{gross}^- &= pR_{ceded}^- \times 1.02 \\ &= 360,000 \times 1.02 = 367,200 \end{aligned}$$

The hard part of this problem is calculating the commutation price P:

$$\begin{aligned} pP_{gross}^- &= \text{primary insurer PAID LOSS direct} = pU_{gross}^- - pR_{gross}^- \\ &= 1,840,000 - 1,200,000 \\ &= 640,000 \\ pP_{ceded}^- &= \text{primary insurer PAID LOSS ceded} = pP_{gross}^- \times qs\% \\ &\text{(also equals } reP_{gross}^-) = 640,000 \times 30\% \\ &= 192,000 \\ &= reP_{gross}^- \text{ (reinsurer PAID LOSS gross)} \\ reU_{gross}^- &= \text{reinsurer ULTIMATE LOSS gross} = reP_{gross}^- + reR_{gross}^- \\ &= 192,000 + 367,200 \\ &= 559,200 \end{aligned}$$

But this is the GROSS ultimate loss PRIOR to commutation. **AFTER** commutation, we have:

$$\begin{aligned} reU_{gross}^+ &= \text{reinsurer ULTIMATE LOSS gross} = reU_{gross}^- \times 104\% \\ &= 559,200 \times 104\% \\ &= 581,568 \end{aligned}$$

now, reinsurer's reserve goes to 0, and the "extra" money in the ultimate must be the commutation price:

$$\begin{aligned} \text{price} &= 581,568 - 192,000 \\ &= 389,568 \end{aligned}$$

We now have what we need to substitute into the **given formulas** for change in taxable income:

$$\begin{aligned} \text{change in taxable income for primary insurer} &= 79,968 \text{ (increase)} \\ \text{change in taxable income for reinsurer} &= -55,416 \text{ (decrease)} \end{aligned}$$