

Reading: Klann.ReinsComm
Model: 2016.Spring #27
Problem Type: mutually beneficial commutation price

(Klann - practice 01) a-Question

Given

gross paid loss	4.1	
gross reserves (case + IBNR)	4.9	
gross discounted reserves (case + IBNR)	3.6	<== economic discount
ceded paid loss	0.4	
ceded reserves (case + IBNR)	2.5	
ceded discounted reserves (case + IBNR)	1.8	<== economic discount

The following discount factors are for **tax purposes**:

	primary insurer	reinsurer	
average discount factor	0.840	0.860	<== for statutory discounting
tax rate	31%	17%	

The reinsurer's assumed losses equal the primary insurer's ceded losses

Calculate

range of the mutually beneficial commutation price (if possible)

We need to solve these 2 inequalities for 'price' and HOPE that the solution ranges overlap.

(If the solution ranges do NOT overlap then there is no MUTUALLY beneficial commutation price)

(A)	price	-	${}_pR_c$	+	${}_pT$	>	0	<== for primary insurer
(B)	- price	+	${}_{re}R_g$	+	${}_{re}T$	>	0	<== for reinsurer

Now:

$${}_pR_c = 1.8 \quad \text{<== use company discounted reserves (economic value)}$$

$${}_{re}R_g = 1.8 \quad \text{<== use company discounted reserves (economic value)}$$

For the primary insurer:

$$\begin{aligned} {}_pT &= \text{tax rate} \times (\text{decrease in taxable income for primary insurer}) \\ &= \text{tax rate} \times (\text{reserves commuted} - \text{price}) \\ &= 31\% \times (2.100 - \text{price}) \end{aligned}$$

where: reserves commuted

$$\begin{aligned} &= \text{undiscounted ceded reserves} \times \text{discount factor} \quad \text{<== tax discounting} \\ &= 2.5 \times 0.840 \\ &= 2.100 \end{aligned}$$

Using these values to solve inequality (A) gives:

$$\text{price} > 1.665 \quad \text{<== for insurer's benefit}$$

And a similar calculation for the reinsurer is as follows:

$$\begin{aligned} {}_{re}T &= \text{tax rate} \times (\text{decrease in taxable income for primary insurer}) \\ &= \text{tax rate} \times (-\text{reserves commuted} + \text{price}) \\ &= 17\% \times (-2.150 + \text{price}) \end{aligned}$$

where: -reserves commuted

$$\begin{aligned} &= -\text{undiscounted ceded reserves} \times \text{discount factor} \quad \text{<== tax discounting} \\ &= -2.5 \times 0.860 \\ &= -2.150 \end{aligned}$$

Using these values to solve inequality (B) gives:

$$\text{price} < 1.728 \quad \text{<== for reinsurer's benefit}$$

Final price range:

$$(1.665, 1.728)$$

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(Klann - practice 02) a-Question

Given

gross paid loss	3.9	
gross reserves (case + IBNR)	4.9	
gross discounted reserves (case + IBNR)	3.4	<== economic discount
ceded paid loss	0.4	
ceded reserves (case + IBNR)	2.8	
ceded discounted reserves (case + IBNR)	2.5	<== economic discount

The following discount factors are for **tax purposes**:

	primary insurer	reinsurer	
average discount factor	0.850	0.890	<== for statutory discounting
tax rate	35%	18%	

The reinsurer's assumed losses equal the primary insurer's ceded losses

Calculate

range of the mutually beneficial commutation price (if possible)

We need to solve these 2 inequalities for 'price' and HOPE that the solution ranges overlap.

(If the solution ranges do NOT overlap then there is no MUTUALLY beneficial commutation price)

(A)	price	-	${}_pR_c$	+	${}_pT$	>	0	<== for primary insurer
(B)	- price	+	${}_{re}R_g$	+	${}_{re}T$	>	0	<== for reinsurer

Now:

$${}_pR_c = 2.5 \quad \text{<== use company discounted reserves (economic value)}$$

$${}_{re}R_g = 2.5 \quad \text{<== use company discounted reserves (economic value)}$$

For the primary insurer:

$${}_pT = \text{tax rate} \times (\text{decrease in taxable income for primary insurer})$$

$$= \text{tax rate} \times (\text{reserves commuted} - \text{price})$$

$$= 35\% \times (2.380 - \text{price})$$

where: reserves commuted

$$= \text{undiscounted ceded reserves} \times \text{discount factor} \quad \text{<== tax discounting}$$

$$= 2.8 \times 0.850$$

$$= 2.380$$

Using these values to solve inequality (A) gives:

price	>	2.565	<== for insurer's benefit
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And a similar calculation for the reinsurer is as follows:

$${}_{re}T = \text{tax rate} \times (\text{decrease in taxable income for primary insurer})$$

$$= \text{tax rate} \times (-\text{reserves commuted} + \text{price})$$

$$= 18\% \times (-2.492 + \text{price})$$

where: -reserves commuted

$$= -\text{undiscounted ceded reserves} \times \text{discount factor} \quad \text{<== tax discounting}$$

$$= -2.8 \times 0.890$$

$$= -2.492$$

Using these values to solve inequality (B) gives:

price	<	2.502	<== for reinsurer's benefit
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Final price range:

(no overlap	,	no overlap)
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Reading: Klann.ReinsComm
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(Klann - practice 03) a-Question

Given

gross paid loss	4.2	<== economic discount
gross reserves (case + IBNR)	5.4	
gross discounted reserves (case + IBNR)	3.3	
ceded paid loss	0.5	<== economic discount
ceded reserves (case + IBNR)	2.9	
ceded discounted reserves (case + IBNR)	1.8	

The following discount factors are for **tax purposes**:

	primary insurer	reinsurer	<== for statutory discounting
average discount factor	0.880	0.870	
tax rate	34%	18%	

The reinsurer's assumed losses equal the primary insurer's ceded losses

Calculate

range of the mutually beneficial commutation price (if possible)

We need to solve these 2 inequalities for 'price' and HOPE that the solution ranges overlap.

(If the solution ranges do NOT overlap then there is no MUTUALLY beneficial commutation price)

(A)	price	-	${}_pR_c$	+	${}_pT$	>	0	<== for primary insurer
(B)	- price	+	${}_{re}R_g$	+	${}_{re}T$	>	0	<== for reinsurer

Now:

$${}_pR_c = 1.8 \quad \text{<== use company discounted reserves (economic value)}$$

$${}_{re}R_g = 1.8 \quad \text{<== use company discounted reserves (economic value)}$$

For the primary insurer:

$$\begin{aligned} {}_pT &= \text{tax rate} \times (\text{decrease in taxable income for primary insurer}) \\ &= \text{tax rate} \times (\text{reserves commuted} - \text{price}) \\ &= 34\% \times (2.552 - \text{price}) \end{aligned}$$

where: reserves commuted

$$\begin{aligned} &= \text{undiscounted ceded reserves} \times \text{discount factor} \quad \text{<== tax discounting} \\ &= 2.9 \times 0.880 \\ &= 2.552 \end{aligned}$$

Using these values to solve inequality (A) gives:

$$\text{price} > 1.413 \quad \text{<== for insurer's benefit}$$

And a similar calculation for the reinsurer is as follows:

$$\begin{aligned} {}_{re}T &= \text{tax rate} \times (\text{decrease in taxable income for primary insurer}) \\ &= \text{tax rate} \times (-\text{reserves commuted} + \text{price}) \\ &= 18\% \times (-2.523 + \text{price}) \end{aligned}$$

where: -reserves commuted

$$\begin{aligned} &= -\text{undiscounted ceded reserves} \times \text{discount factor} \quad \text{<== tax discounting} \\ &= -2.9 \times 0.870 \\ &= -2.523 \end{aligned}$$

Using these values to solve inequality (B) gives:

$$\text{price} < 1.641 \quad \text{<== for reinsurer's benefit}$$

Final price range:

$$(1.413, 1.641)$$

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(Klann - practice 04) a-Question

Given

gross paid loss	3.7	<== economic discount
gross reserves (case + IBNR)	4.6	
gross discounted reserves (case + IBNR)	3.6	
ceded paid loss	0.7	<== economic discount
ceded reserves (case + IBNR)	2.9	
ceded discounted reserves (case + IBNR)	2.1	

The following discount factors are for **tax purposes**:

	primary insurer	reinsurer	<== for statutory discounting
average discount factor	0.860	0.810	
tax rate	32%	18%	

The reinsurer's assumed losses equal the primary insurer's ceded losses

Calculate

range of the mutually beneficial commutation price (if possible)

We need to solve these 2 inequalities for 'price' and HOPE that the solution ranges overlap.

(If the solution ranges do NOT overlap then there is no MUTUALLY beneficial commutation price)

(A)	price	-	${}_pR_c$	+	${}_pT$	>	0	<== for primary insurer
(B)	- price	+	${}_{re}R_g$	+	${}_{re}T$	>	0	<== for reinsurer

Now:

$${}_pR_c = 2.1 \quad \text{<== use company discounted reserves (economic value)}$$

$${}_{re}R_g = 2.1 \quad \text{<== use company discounted reserves (economic value)}$$

For the primary insurer:

$${}_pT = \text{tax rate} \times (\text{decrease in taxable income for primary insurer})$$

$$= \text{tax rate} \times (\text{reserves commuted} - \text{price})$$

$$= 32\% \times (2.494 - \text{price})$$

where: reserves commuted

$$= \text{undiscounted ceded reserves} \times \text{discount factor} \quad \text{<== tax discounting}$$

$$= 2.9 \times 0.860$$

$$= 2.494$$

Using these values to solve inequality (A) gives:

$$\text{price} > 1.915 \quad \text{<== for insurer's benefit}$$

And a similar calculation for the reinsurer is as follows:

$${}_{re}T = \text{tax rate} \times (\text{decrease in taxable income for primary insurer})$$

$$= \text{tax rate} \times (-\text{reserves commuted} + \text{price})$$

$$= 18\% \times (-2.349 + \text{price})$$

where: -reserves commuted

$$= -\text{undiscounted ceded reserves} \times \text{discount factor} \quad \text{<== tax discounting}$$

$$= -2.9 \times 0.810$$

$$= -2.349$$

Using these values to solve inequality (B) gives:

$$\text{price} < 2.045 \quad \text{<== for reinsurer's benefit}$$

Final price range:

$$(1.915, 2.045)$$